

PythonTip 03 - Recursion

February 15, 2023

1 Recursion

A recursive algorithm is an algorithm that calls itself. You need a base case so you don't get stuck in an infinite loop.

Example: suppose we want to calculate the quantity $n! = n(n - 1)(n - 2) \cdots 3 \cdot 2 \cdot 1$.

$$5! = 5 * 4 * 3 * 2 * 1 = 120$$

We'll use the fact that $n! = n \cdot (n - 1)!$.

```
[1]: # What's wrong with this function?
def factorial(n):
    return n * factorial(n-1)
```

```
[2]: factorial(3)
```

```
-----
RecursionError                                     Traceback (most recent call last)
Cell In[2], line 1
----> 1 factorial(3)

Cell In[1], line 3, in factorial(n)
      2 def factorial(n):
----> 3     return n * factorial(n-1)

Cell In[1], line 3, in factorial(n)
      2 def factorial(n):
----> 3     return n * factorial(n-1)

[... skipping similar frames: factorial at line 3 (2970 times)]

Cell In[1], line 3, in factorial(n)
      2 def factorial(n):
----> 3     return n * factorial(n-1)

RecursionError: maximum recursion depth exceeded
```

What calls are happening?

```
[ ]: # What's wrong with this function?  
def factorial(n):  
    return n * factorial(n-1)
```

```
factorial(3)  
-> 3 * factorial(2)  
-> 3 * 2 * factorial(1)  
-> 3 * 2 * 1 * factorial(0)  
-> 3 * 2 * 1 * 0 * factorial(-1)  
-> infinite recursion
```

```
[14]: # We need a base case!  
def factorial(n):  
    assert n >= 0 and isinstance(n, int), "invalid input into factorial"  
    if n == 1:  
        # factorial(1) = 1  
        return 1  
    return n * factorial(n-1)
```

```
[15]: factorial(3.5)
```

```
-----  
AssertionError                                                 Traceback (most recent call last)  
Cell In[15], line 1  
----> 1 factorial(3.5)  
  
Cell In[14], line 3, in factorial(n)  
      2     def factorial(n):  
----> 3         assert n >= 0 and isinstance(n, int), "invalid input into factorial"  
      4         if n == 1:  
      5             # factorial(1) = 1  
      6             return 1  
  
AssertionError: invalid input into factorial
```

```
factorial(5)  
5 * factorial(4)  
5 * (4 * factorial(3))  
5 * (4 * (3 * factorial(2)))  
5 * (4 * (3 * (2 * factorial(1))))  
5 * (4 * (3 * (2 * 1)))
```

```
[9]: factorial(-1)
```

```
-----  
RecursionError                                                 Traceback (most recent call last)
```

```
Cell In[9], line 1
----> 1 factorial(-1)

Cell In[3], line 6, in factorial(n)
3 if n == 1:
4     # factorial(1) = 1
5     return 1
----> 6 return n * factorial(n-1)

Cell In[3], line 6, in factorial(n)
3 if n == 1:
4     # factorial(1) = 1
5     return 1
----> 6 return n * factorial(n-1)

[... skipping similar frames: factorial at line 6 (2971 times)]

Cell In[3], line 6, in factorial(n)
3 if n == 1:
4     # factorial(1) = 1
5     return 1
----> 6 return n * factorial(n-1)

RecursionError: maximum recursion depth exceeded
```

[]: